IIT-JEE/NEET/NTSE/FOUNDATION COURSE

JEE (Main)-2024 : Phase-1 (31-01-2024)-Evening

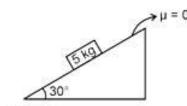
PHYSICS

SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which ONLY ONE is correct.

Choose the correct answer:

 For the block shown, F₁ is the minimum force required to move block upwards and F₂ is the minimum force required to prevent it from slipping, find |F₁ - F₂|



- (1) 50√3 N
- (2) 5√3 N
- (3) 25√3 N
- (4) $\frac{5\sqrt{3}}{2}$ N

Answer (2)

Sol. $f_K = \mu mg \cos \theta$

$$= 0.1 \times \frac{50 \times \sqrt{3}}{2}$$

$$F_1 = mg \sin\theta + f_K$$

$$= 25 + 2.5\sqrt{3}$$

$$F_2 = mg \sin\theta - f_K$$

$$= 25 - 2.5\sqrt{3}$$

$$F_1 - F_2 = 5\sqrt{3} \text{ N}$$

- Force on a particle moving in straight line is given by F = 6t²î - 3tĵ and velocity is v = 3t²î + 6tĵ. Find power at t = 2.
 - (1) 216 W
 - (2) 108 W
 - (3) 0 W
 - (4) 54 W

Answer (1)

Sol. P = F · V

$$=18t^4-18t^2$$

$$\Rightarrow P(t=2)=18[16-4]=216 \text{ W}$$

- 3. If $E = \frac{A x^2}{Bt}$ where E is energy, x is displacement and t is time. Find dimensions of AB
 - (1) [M-1L2T]
 - (2) [ML2T-1]
 - (3) [M-1L2T-2]
 - (4) [ML2T-2]

Answer (1)

Sol. $[A] = L^2$

$$B = \frac{x^2}{tE} = \frac{L^2}{TML^2T^{-2}} = \frac{1}{MT^{-1}}$$

$$[AB] = [M^{-1}L^{2}T]$$

- Unpolarised light incident on transparent glass at incident angle 60°. If reflected ray is completely polarised, then angle of refraction is
 - (1) 45°
 - (2) 60°
 - (3) 30°
 - (4) 37°

Answer (3)

Sol. By Brewsters law

$$\mu = \tan i$$

$$u = \sqrt{3}$$

$$1 \times \frac{\sqrt{3}}{2} = \sqrt{3} \times \sin r$$

$$\sin r = \frac{1}{2}$$

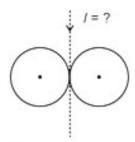
$$r = 30^{\circ}$$

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Two solid spheres each of mass 2 kg and radius 75 cm are arranged as shown. Find MOI of the system about the given axis.



- (1) 3.15 kg m²
- (2) 31.5 kg m²
- (3) 0.9 kg m²
- (4) 9 kg m²

Answer (1)

Sol.
$$I = \left(\frac{2}{5}MR^2 + MR^2\right) \times 2$$

$$=\frac{14}{5}\times2\times\frac{9}{16}$$

$$=\frac{63}{20}$$

- 6. If the current through an incandescent lamp decreases by 20%, how much change will be there in its illumination?
 - (1) 36%
- (2) 64%
- (3) 20%
- (4) 40%

Answer (1)

Sol.
$$p = i^2 R$$

$$p' = 0.64 i^2 R$$

- 7. Find the speed of sound in oxygen gas at STP.
 - (1) 300 m/s
 - (2) 350 m/s
 - (3) 330 m/s
 - (4) 400 m/s

Answer (3)

Sol.
$$v = \sqrt{\frac{\gamma RT}{M}} = 330 \text{ m/s}$$

 Find average power in electric circuit if source voltage (V) = 20sin(100ωt) and current in the circuit

$$(I) = 2\sin(100\omega t + \frac{\pi}{3})$$

- (1) 10 W
- (2) 20 W
- (3) 5 W
- (4) 15.5 W

Answer (1)

$$=\frac{20}{\sqrt{2}}\times\frac{2}{\sqrt{2}}\times\cos 60^\circ$$

- = 10 W
- In a photoelectric experiment, frequency f = 1.5f₀
 (f₀: threshold frequency). If the frequency of light is changed to f/2, then photocurrent becomes (intensity of light has doubled)
 - (1) Zero
 - (2) Doubled
 - (3) Same
 - (4) Thrice

Answer (1)

Sol. Since
$$\frac{f}{2} < f_0$$

- Radius of curvature of equiconvex lens is 20 cm.
 Material of lens is having refractive index of 1.5. Find image distance from lens if an object is placed 10 cm away from the lens.
 - (1) 20 cm
 - (2) 10 cm
 - (3) 40 cm
 - (4) 5 cm

Answer (1)

Sol.
$$\frac{1}{f} = (\mu - 1) \left(\frac{2}{R} \right)$$
 $f = 20 \text{ cm}$

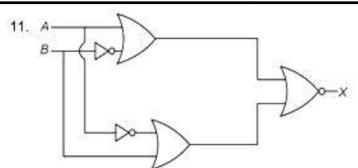
$$\frac{1}{v} - \frac{1}{u} = \frac{1}{f}$$

$$\frac{1}{v} + \frac{1}{10} = \frac{1}{20}$$

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Draw truth table of given gate circuit.

Answer (2)

Sol.
$$X = (A + \overline{B}) + (\overline{A} + B)$$

$$(A+B)\cdot (A+B)$$

$$(\bar{A} \cdot B) \cdot (A \cdot \bar{B}) = \bar{A} \cdot B \cdot A \cdot \bar{B} = 0$$

- 12. The magnetic flux through a loop varies with time as $\phi = 5t^2 - 3t + 5$. If the resistance of loop is 8 Ω , find the current through it at t = 2 s
 - (1) $\frac{15}{9}$ A
- (2) $\frac{5}{9}$ A
- (3) $\frac{17}{8}$ A (4) $\frac{13}{8}$ A

Answer (3)

Sol.
$$\frac{d\phi}{dt} = 10t - 3$$

at
$$t = 2$$
. $V = 17$

$$i = \frac{V}{R} = \frac{17}{8} A$$

- 13. 8 moles of oxygen and 4 moles of nitrogen are at same temperature T and are mixed. The total interna energy is
 - 60RT
 - (2) 15RT
 - (3) 30RT
 - (4) 90RT

Answer (3)

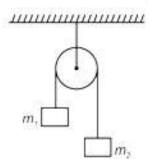
Sol.
$$U = nC_{o}T$$

$$\Rightarrow U = n_1 C_{V_1} T + n_2 C_{V_2} T$$

$$\Rightarrow 8 \times \frac{5R}{2} \times T + 4 \times \frac{5R}{2} \times T$$

$$=30RT$$

14. In the system shown below, the pulley 4 string are ideal. If the acceleration of blocks is $\frac{g}{8}$, find $\frac{m_1}{m_2}$



Answer (1)

Sol.
$$a = \frac{(m_1 - m_2)g}{(m_1 + m_2)} = \frac{g}{8}$$

$$8m_1 - 8m_2 = m_1 + m_2$$

$$7m_1 = 9m_2$$

$$\frac{m_1}{m_2} = \frac{9}{7}$$



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- 15. The force between two charged particle placed in air at separation x is F₀. Both the charged particle immerged in a medium of dielectric constant K without changing separation between two charge, then net force on one of the particle is now
 - (1) $\frac{F_0}{K}$
 - (2) $\frac{F_0}{2K}$
 - (3) $\frac{2F_0}{K}$
 - (4) F_0

Answer (1)

Sol. In air
$$F = \frac{1}{4\pi} = \frac{q_1 q_2}{r_2}$$

In medium
$$F' = \frac{1}{4\pi(k \in 0)} \frac{q_1 q_2}{r^2}$$

$$F' = \frac{F_0}{K}$$

- Two vector each of magnitude A are inclined at angle θ with each other, then magnitude of resultant vector is
 - (1) $A \cos^2 \frac{\theta}{2}$
 - (2) $2A\cos\frac{\theta}{2}$
 - (3) 2A cosθ
 - (4) $A\cos\frac{\theta}{2}$

Answer (2)

Sol. The magnitude of resultant vector (R) = $\sqrt{a^2 + b^2 + 2ab\cos\theta}$

here a = b = A

then
$$R = \sqrt{A^2 + A^2 + 2A^2 \cos \theta}$$

$$= A\sqrt{2} \sqrt{1 + \cos \theta}$$

$$= \sqrt{2}A \sqrt{2\cos^2 \frac{\theta}{2}}$$

$$= 2A\cos \frac{\theta}{2}$$

 Statement 1 : Electric and magnetic energy density in electromagnetic waves are equal.

Statement 2: Electromagnetic waves exert pressure on a surface.

- Statement 1 is true & Statement 2 is true and is correct explanation of Statement 1
- (2) Statement 1 is true & Statement 2 is true but is not correct explanation of Statement 1
- (3) Statement 1 is true but Statement 2 is false
- (4) Statement 1 is false but Statement 2 is true

Answer (2)

Sol.
$$\frac{1}{2} \varepsilon_0 E^2 = \frac{B^2}{2\mu_0}$$

$$\therefore$$
 E = CB and C = $\frac{1}{\mu_0 \epsilon_0}$

- A pendulum completes 50 oscillations in 40 seconds.
 If the length of pendulum is (20 ± 0.2) cm and resolution of watch is 1 second, find the percentage error in calculation of g.
 - (1) 7%
 - (2) 3%
- **(3)** 6%
 - (4) 4%

Answer (3)

Sol.
$$T = 2\pi \sqrt{\frac{I}{g}}$$

$$g = \frac{4\pi^2 I}{T^2}$$

$$\frac{\Delta g}{g} = \frac{\Delta l}{l} + \frac{2\Delta T}{T}$$

$$= \frac{0.2}{20} + 2\left(\frac{1}{40}\right)$$

19.

20.

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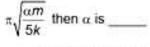


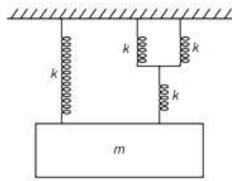
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SECTION - B

Numerical Value Type Questions: This section contains 10 Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

21. The period of oscillation of system shown below is





Answer (12)

Sol.
$$k_{eq} = \frac{2k \cdot k}{3k} + k = \frac{5k}{3}$$

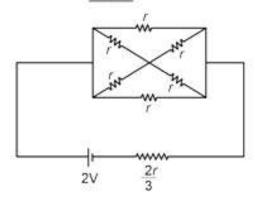
Angular frequency of oscillation (ω) = $\sqrt{\frac{k_{eq}}{m}}$

$$\omega = \sqrt{\frac{5k}{3m}}$$

Period of oscillation
$$(\tau) = \frac{2\pi}{\omega} = 2\pi \sqrt{\frac{3m}{5k}}$$

$$= \pi \sqrt{\frac{12m}{5k}}$$

 In the given circuit, r = 2 Ω. The power dissipated in the circuit is
 W.



Answer (2)

Sol. $R_{eq} = r$

$$\therefore P = \frac{V^2}{r} = \frac{4}{2} = 2 \text{ W}$$

23. A body of mass m is projected with speed u at angle 45° with horizontal. The angular momentum of body, about point of projection when body is at highest point, is √2 m u³ find x,

Answer (8)

Sol.
$$L = mu \cos \theta \frac{u^2 \sin^2 \theta}{2g}$$

= $mu^3 \frac{1}{4\sqrt{2} a} \Rightarrow x = 8$

24. Mass of moon is ¹/₈₁ times the mass of a planet and radius is ¹/₉ times the radius of the planet. The ratio of escape speed from planet to escape speed from moon is _____.

Answer (3)

Sol.
$$v_{\rm esc} = \sqrt{\frac{2 GM}{R}}$$

$$\Rightarrow$$
 Ratio = $\sqrt{\frac{81}{9}}$ = 3

 Find the mass number of an atom whose radius is half of that of a given atom of mass number 192.

Answer (24)

Sol.
$$r = R_0 (192)^{\frac{1}{3}}$$

$$\frac{r}{2} = R_0(m)^{\frac{1}{3}}$$

$$m=\frac{192}{8}=24$$

26.

27.

28.

29.

30.



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CHEMISTRY

SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which ONLY ONE is correct.

Choose the correct answer:

Statement 1: Se disproportionate into H2S2O3 and S2- in alkaline medium

Statement 2: CIO₂ undergoes disproportionation in acidic medium.

- (1) Statement 1 is correct but statement 2 is
- (2) Statement 1 is incorrect but statement 2 is correct
- (3) Both statement 1 and statement 2 are correct
- (4) Both statement 1 and statement 2 are incorrect

Answer (1)

Oxidation Sol. (1) S, + NaOH -> Na,S + Na,S,O, Reduction

> (2) Cl is in its highest oxidation state (+7). It cannot be further oxidised

> Therefore, statement 1 is correct but statement 2 is incorrect.

- 2. Which of the following is correct?
 - (1) [NiCl₄]2- diamagnetic [Ni(CO)₄] – diamagnetic
 - (2) [Ni(CO)₄] diamagnetic [NiCl₄]²⁻ – paramagnetic
 - (3) [NiCl₄]²⁻ paramagnetic [Ni(CO)₄] - paramagnetic
 - (4) [NiCl₄]²⁻ paramagnetic [Ni(CO)₄] – diamagnetic

Answer (2)

Sol. Ni2+: 4s03d0 (No pairing with Cl-) [Ni(CO)₄]: 4s°3d¹⁰ (diamagnetic)

3. Statement-I: Among 15th group hydrides reducing character decreases from NH₃ to BiH₃.

Statement-II: E₂O₃ and E₂O₅ are always basic.

[Where E is group 15 element]

- (1) Both statement-I and Statement-II are correct
- (2) Statement-I is correct and Statement-II is false
- (3) Statement-I is false and Statement-II is correct
- (4) Both Statement-I and Statement-II are false

Answer (4)

Sol. Reducing character increases from NH₃ to BiH₃. Group 15 oxides of type E2O3 and E2O5 are not always basic.

- Which of the following has maximum ionic character?
 - (1) KCI
- (2) AgCI
- (3) CoCl₂
- (4) BaCl₂

Answer (1)

Charge Sol. Polarisation power x

> for K*, polarising power is least and ionic character is maximum.

- Match the following:
 - (a) [Cr(H₂O)₆]+3
- (i) t₂₀eg^o
- (b) [Fe(H₂O)₆]+3
- (ii) t₃,eg°
- (c) [Ni(H₂O)₆]+2
- (iii) t₂₀eg²
- (d) [V(H₂O)₆]*³
- (iv) t₂₀⁶ eg²
- (1) (a)-(ii), (b)-(iii), (c)-(iv), (d)-(i)
- (2) (a)-(iii), (b)-(iv), (c)-(i), (d)-(ii)
- (3) (a)-(iv), (b)-(ii), (c)-(iii), (d)-(i)
- (4) (a)-(ii), (b)-(iv), (c)-(i), (d)-(iii)

Answer (1)

Sol. (a) $[Cr(H_2O)_6]^{*3} \rightarrow Cr^{*3} \rightarrow t_{2\alpha}^3 eg^{\alpha}$

(b) $[Fe(H_2O)_6]^{*3} \rightarrow Fe^{3*} \rightarrow t_{2a}^3 eg^2$

(c) $[Ni(H_2O)_6]^{*2} \rightarrow Ni^{2*} \rightarrow t_{2a}^6 eg^2$

(d) $[V(H_2O)_6]^{*3} \rightarrow V^{3*} \rightarrow t_{2a}^2 eg^{\circ}$

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Quantum number for outermost electron of K-atom are given by

(1)
$$n = 4$$
, $l = 0$, $m = 0$, $s = \frac{1}{2}$

(2)
$$n = 4$$
, $l = 1$, $m = 0$, $s = \frac{1}{2}$

(3)
$$n = 3$$
, $l = 0$, $m = 0$, $s = \frac{1}{2}$

(4)
$$n = 4$$
, $l = 0$, $m = 1$, $s = \frac{1}{2}$

Answer (1)

Sol. K₁₉ = 1s²2s²2p⁶3s²3p⁶4s¹

For 4s electron

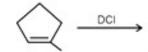
$$n = 4$$

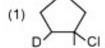
$$I = 0$$

$$m = 0$$

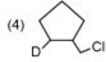
$$s = \frac{1}{2}$$

7. What is the product formed in the below given reaction?

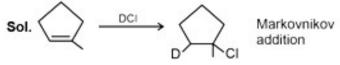






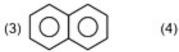


Answer (1)



8. What is the major product formed in the following reaction?

$$\bigcirc + \bigcirc \stackrel{\circ}{|} \stackrel{\text{Cl}}{\underset{\text{AlCl}_3}{}} ?$$

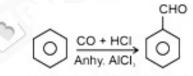


(4)

Answer (1)

Sol.

Identify the given rection



- Rosenmund reaction
- (2) Stephen reaction
- (3) Gattemann Koch reaction
- (4) Etard reaction

Answer (3)

Sol. The given reaction is Gattemann Koch reaction.

- Choose the correct answers.
 - (A) Mn₂O₇ is a oil at room temperature.
 - (B) V₂O₄ react with acid to give VO²⁺
 - (C) CrO is a basic oxide
 - (D) V₂O₅ does not react with acids.
 - (1) A, B and C only
- (2) B, C and D only
- (3) A only
- (4) B and C only

Answer (1)

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Sol. A, B and C are correct.

- Mn₂O₇ is a green oil at room temperature.
- V₂O₄ react with acids to give VO²⁺.
- CrO is Basic and CrO₃ is acidic.
- V₂O₅ react with acids as well as alkali.

(Ref. NCERT Pg 224)

11. Consider the following reaction:

A and B respectively are

(1)
$$A = O_2N + O_2$$

$$O_2N + O_3N +$$

(2)
$$A = \bigcirc OH$$

 NO_2 $B = \bigcirc OH$
 NO_2

(3)
$$A = \bigcup_{NO_2}^{Br} NO_2$$
 $B = \bigcup_{NO_2}^{OH} NO_2$

(4)
$$A = \bigcup_{NO_2}^{Bf} NO_2$$
, $B = \bigcup_{NO_3}^{OH}$

Answer (2)

Sol.
$$\bigcirc$$

Conc. HNO_3
Conc. H_3SO_4
 $[Ndration]$
 OH

(i) NaOH, 573 K
(ii) dil. HCI
 OH
 O

12. What will be the reactivity order of following compounds towards electrophilic substitution reaction?

- (1) 1 > 3 > 2 > 4
- (2) 4 > 1 > 2 > 3
- (3) 3 > 2 > 1 > 4
- (4) 4 > 3 > 1 > 2

Answer (2)

Sol.
$$\langle \bigcirc \rangle$$
—CH₃ \Rightarrow activating (+I)

$$\bigcirc$$
 NO₂ \Rightarrow (-M) \Rightarrow strongly deactivating

- Correct IUPAC structure for the given organic compound is
 - 2,2-Dibromo-1-phenylpentane

Answer (2)

 Statement-I: Aniline on reaction with concentrated H₂SO₄ at 475 K gives p-amino benzene sulphonic acid. This gives blood red colour with Lassaigne's test.

Statement-II: Aniline forms a salt with anhydrus AICI₃ in Friedel Craft's reaction.



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- Both Statement-I and Statement-II are correct
- (2) Both Statement-I and Statement-II are incorrect
- (3) Statement-I is correct and Statement-II incorrect
- (4) Statement-I is incorrect and Statement-II

Answer (1)

p-amino benzene sulphonic acid contains both N and S, so it gives blood red colour with Lassaigne's

Consider the following reaction.

Select P

(Where Me is CH₃)

SO.Na

Answer (1)

is an example of azo coupling reaction and fina product is methyl orange.

16.
$$A(g) \rightleftharpoons B(g) + \frac{1}{2}C(g)$$

In the about reaction, the correct relation between K_p , α and equilibrium pressure (p) is

(1)
$$K_p = \frac{\alpha^{\frac{1}{2}} 2p^{\frac{1}{2}}}{(2+\alpha)^{\frac{1}{2}}}$$

(2)
$$K_p = \frac{\alpha^{\frac{1}{2}} p^{3/2}}{(2+\alpha)^{3/2}}$$

(3)
$$K_p = \frac{\alpha^{1/2} 2p^{1/2}}{(2+\alpha)^{3/2}}$$

(4)
$$K_p = \frac{\alpha^{3/2} p^{1/2}}{(2+\alpha)^{3/2} (1-\alpha)}$$

Answer (4)

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Sol.

$$A(g) \implies B(g) + \frac{1}{2}(g)$$

Initial r moles 0 (

Eqb.
$$n(1 - \alpha)$$
 $n\alpha$ $\frac{n\alpha}{2}$

total moles = $n(1+\alpha)$

Eqb.
$$\frac{(1-\alpha)p}{1+\frac{\alpha}{2}}$$
 $\frac{\alpha p}{1+\frac{\alpha}{2}}$ $\frac{\left(\frac{\alpha}{2}\right)p}{1+\frac{\alpha}{2}}$

$$\frac{K_{p} = \frac{\alpha p}{\left(1 + \frac{\alpha}{2}\right)} \times \left[\frac{\alpha p}{\left(2 + \alpha\right)}\right]^{\frac{1}{2}}}{\frac{\left(1 - \alpha\right)p}{1 + \frac{\alpha}{2}}}$$

$$K_p = \frac{\alpha^{3/2} p^{1/2}}{(2+\alpha)^{3/2} (1-\alpha)}$$

17.

18.

19. 20.

SECTION - B

Numerical Value Type Questions: This section contains 10 Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

 Half life of a first order reaction is 36 hr. Find out time (in hr) required for concentration of reactant to get reduced by 90%.

Answer (120)

Sol.
$$t_{90} = \frac{2.303}{k} \log \left(\frac{100}{100 - 90} \right)$$

= $\frac{2.303 \times 36}{2.303 \times \log 2} \times \log 10 = \frac{36}{0.3} = 120$

 A 1 mol ideal gas expands from 10 L to 100 L at 300 k, if above expansion takes place reversibly and isothermally then magnitude of work done is (in KJ)

Answer (06)

Sol.
$$w = -nRT \ln \frac{V_2}{V_1}$$

$$|w| = 2.303 \text{ nRT log} \frac{V_2}{V_1}$$

$$|w| = 1 \times 2.303 \times 8.314 \times 300 \log \frac{100}{10}$$

|w| = 5744 J

 $|w| = 5.744 \text{ kJ} \approx 6 \text{ kJ}$

23. How many of the following vitamins are stored in Human Body?

A. B. C. D. E. K?

Answer (4)

Sol. A, D, E, K vitamins are fat soluble vitamins, are stored in liver and adipose tissue.

While vitamin B and vitamin C are water soluble and must be supplied regularly in diet (not stored) (except vitamin B₁₂) (NCERT, Pg: 426)

 Number of moles of H^{*} required by 1 mole MnO₄⁻ to oxidize oxalate ion to CO₂ is

Answer (8)

Sol. The balanced reaction is as follows

$$2MnO_4^- + 5C_2O_4^{2-} + 16H' \rightarrow 2Mn^{2'} + 10CO_2 + 8H_2O$$

2 mole MnO₄ react with 16 mole H⁴

1 mole MnO₄ will react with 8 mole H^{*}

 The potassium chloride is heated with potassium dichromate and conc. sulphuric acid to give products. The oxidation state of chromium in product is (+)_____.

Answer (06.00)

Sol. This is an example of chromyl chloride test

 $K_2Cr_2O_7 + 4KCl + 6H_2SO_4 \rightarrow 6KHSO_4$

+ 2CrO₂Cl₂ + 3H₂O

Oxidation state of Cr is +6.

 Number of structural isomeric products formed by monochlorination of 2-methylbutane in presence of sunlight is

Answer (4)

27.

28

29.

30.

MATHEMATICS

SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which ONLY ONE is correct.

Choose the correct answer:

- $a = \sin^{-1}(\sin 5), b = \cos^{-1}(\cos 5)$ then $a^2 + b^2$ is equal to
 - (1) $8\pi^2 40\pi + 50$
- (2) $4\pi^2 + 25$
- (3) $8\pi^2 50$
- (4) $8\pi^2 + 40\pi + 50$

Answer (1)

Sol. $a = \sin^{-1}(\sin 5) = 5 - 2\pi$

and
$$b = \cos^{-1}(\cos 5) = 2\pi - 5$$

$$a^2 + b^2 = (5 - 2\pi)^2 + (2\pi - 5)^2$$

$$=8\pi^2-40\pi+50$$

- A coin is biased such that head has two chances than tails, what is the probability of getting 2 heads and 1 tail?
- (2) $\frac{2}{29}$

Answer (4)

Sol. Let probability of tail is $\frac{1}{2}$

- ⇒ Probability of getting head = $\frac{2}{3}$
- ... Probability of getting 2 heads and 1 tail

$$= \left(\frac{2}{3} \times \frac{2}{3} \times \frac{1}{3}\right) \times 3$$
$$= \frac{4}{27} \times 3$$
$$= \frac{4}{9}$$

- Let mean and variance of 6 observations a. b. 68. 44, 40, 60 be 55 and 194. If a > b then find a + 3b
 - (1) 211.83
- (2) 201.59
- (3) 189.57

Answer (2)

(4) 198.87

- Sol. $\frac{a+b+68+44+40+60}{6} = 55$
 - 212 + a + b = 330
 - $\Rightarrow a+b=118$
 - $\frac{\sum x_i^2}{2} \left(\overline{x}\right)^2 = 194$
- $\frac{a^2 + b^2 + (68)^2 + (44)^2 + (40)^2 + (60)^2}{6} (55)^2 = 194$
 - = 3219
 - $11760 + a^2 + b^2 = 19314$
 - $\Rightarrow a^2 + b^2 = 19314 11760$
 - = 7554
 - $(a + b)^2 2ab = 7554$

From here b = 41.795

- a + b = 118
- $\Rightarrow a+b+2b=118+83.59$
- = 201.59
- If 2nd, 8th, 44th terms of A.P. are 1st, 2nd and 3rd terms respectively of G.P. and first term of A.P. is 1 ther the sum of first 20 terms of A.P. is
 - (1) 970
- (2) 916
- (3)980
- (4) 990

Answer (1)

Sol. a + d, a + 7d and a + 43d are 1st, 2nd, 3nd term o GP

$$\frac{a+7d}{a+d} = \frac{a+43d}{a+7d}$$

- \Rightarrow $(a + 7d)^2 = (a + d)(a + 43d)$
- $\Rightarrow a^2 + 49d^2 + 14d = a^2 + 44ad + 43d^3$
- \Rightarrow 6d° = 30ad
- $\Rightarrow d^{0} = 5d$
- \Rightarrow d = 0.5
- a = 1, d = 5

$$S_{20} = \frac{20}{2}[2 + (19)5]$$

- = 10 [95 + 2]
- = 970

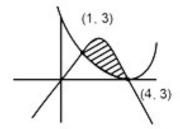
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- The area of the region enclosed by the parabolas $y = 4 - x^2$ and $3y = (x - 4)^2$ is in (sq. unit)?
 - (1) $\frac{14}{3}$
- (2) 4
- (4) 6

Answer (4)



Sol. Area =
$$\left| \int_{1}^{4} \left[(4-x)^{2} - \frac{(x-4)^{2}}{3} \right] dx \right|$$

Area =
$$\left| 4x - \frac{x^3}{3} - \frac{(x-4)^3}{9} \right|^4$$

$$=\left[\left(16-\frac{64}{3}\right)-\left(4-\frac{1}{3}+\frac{27}{9}\right)\right]$$

$$= \left| 16 - \frac{64}{3} - 4 + \frac{1}{3} + 3 \right|$$

$$= |15 - 2| = 6$$

6. If $A \begin{bmatrix} 1 \\ 0 \\ 1 \end{bmatrix} = 2 \begin{bmatrix} 1 \\ 0 \\ 1 \end{bmatrix}$, $A \begin{bmatrix} -1 \\ 0 \\ 1 \end{bmatrix} = 4 \begin{bmatrix} -1 \\ 0 \\ 1 \end{bmatrix}$

and
$$A\begin{bmatrix} 0\\1\\0 \end{bmatrix} = 2\begin{bmatrix} 0\\1\\0 \end{bmatrix}$$
 where, A is a 3 × 3 matrix and

$$(A-3I)$$
 $\begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} -1 \\ 2 \\ 3 \end{bmatrix}$ then the value of (x, y, z) is

- (1) (1, 2, 3)
- (2) (1, -2, 3)
- (3) (1, -2, -3) (4) (-1, -2, -3)

Answer (3)

Sol. Let
$$A = \begin{bmatrix} x_1 & y_1 & z_1 \\ x_2 & y_2 & z_2 \\ x_3 & y_3 & z_3 \end{bmatrix}$$

Given
$$A = \begin{bmatrix} 1 \\ 0 \\ 1 \end{bmatrix} = \begin{bmatrix} 2 \\ 0 \\ 2 \end{bmatrix}$$
 ... (1)

$$\begin{bmatrix} \mathbf{x}_1 + \mathbf{z}_1 \\ \mathbf{x}_2 + \mathbf{z}_2 \\ \mathbf{x}_3 + \mathbf{z}_3 \end{bmatrix} = \begin{bmatrix} 2 \\ 0 \\ 2 \end{bmatrix}$$

 $\therefore x_1 + z_1 = 2$

 $\boldsymbol{x}_2 + \boldsymbol{z}_2 = \boldsymbol{0}$

$$\mathbf{Z}_3 + \mathbf{Z}_3 = \mathbf{0}$$

Given
$$A = \begin{bmatrix} -1 \\ 0 \\ 1 \end{bmatrix} = \begin{bmatrix} -4 \\ 0 \\ 4 \end{bmatrix}$$

$$\therefore \begin{bmatrix}
-\mathbf{x}_1 + \mathbf{z}_1 \\
-\mathbf{x}_2 + \mathbf{z}_2 \\
-\mathbf{x}_3 + \mathbf{z}_3
\end{bmatrix} = \begin{bmatrix} 4 \\ 0 \\ 4 \end{bmatrix}$$

 $\Rightarrow -x_1 + z_1 = -4$

... (5)

$$-\mathbf{x}_2 + \mathbf{z}_2 = \mathbf{0}$$

... (6)

$$-\mathbf{x}_3+\mathbf{z}_3=4$$

Given
$$A = \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix} = \begin{bmatrix} 0 \\ 2 \\ 0 \end{bmatrix}$$

$$y_1 = 0, y_2 = 2, y_3 = 0$$

.: from (2), (3), (4), (5), (6) and (7)

$$x_1 = 3$$
, $x_2 = 0$, $x_3 = -1$

$$y_1 = 0, y_2 = 2, y_3 = 0$$

$$z_1 = -1$$
, $z_2 = 0$, $z_3 = 3$

$$\therefore A = \begin{bmatrix} 3 & 0 & -1 \\ 0 & 2 & 0 \\ -1 & 0 & 3 \end{bmatrix}$$

$$\therefore \text{ Now } (A-3 I) \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} -1 \\ 2 \\ 3 \end{bmatrix}$$

$$\begin{bmatrix} 0 & 0 & -1 \\ 0 & -1 & 0 \\ -1 & 0 & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} -1 \\ 2 \\ 3 \end{bmatrix}$$

$$\begin{bmatrix} -z \\ -y \\ -x \end{bmatrix} = \begin{bmatrix} -1 \\ 2 \\ 3 \end{bmatrix}$$

$$[z=1], [y=-2], [x=-3]$$



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Let $f: R \to (0, \infty)$ be increasing function such that

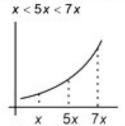
$$\lim_{x \to \infty} \frac{f(7x)}{f(x)} = 1 \text{ then } \lim_{x \to \infty} \left(\frac{f(5x)}{f(x)} - 1 \right) \text{ is equal to}$$

(1) Zero

(3) 1

Answer (1)

Sol. f is increasing function



f(x) < f(5x) < f(7x)

$$\frac{f(x)}{f(x)} < \frac{f(5x)}{f(x)} < \frac{f(7x)}{f(x)}$$

$$\lim_{x \to \infty} \frac{f(x)}{f(x)} < \lim_{x \to \infty} \frac{f(5x)}{f(x)} < \lim_{x \to \infty} \frac{f(7x)}{f(x)}$$

$$1 < \lim_{x \to \infty} \frac{f(5x)}{f(x)} < 1 \quad \Rightarrow \lim_{x \to \infty} \frac{f(5x)}{f(x)} = 1$$

$$\lim_{x\to\infty}\left(\frac{f(5x)}{f(x)}-1\right)=0$$

Let z₁ and z₂ be two complex numbers such that $z_1 + z_2 = 5$ and $z_1^3 + z_2^3 = 20 + 15i$, then the value of $z_1^4 + z_2^4$ is equal to

(1)75

(2) 25√5

(3) 15√15

(4) 30√3

Answer (1)

Sol. $z_1 + z_2 = 5$

$$z_1^3 + z_2^3 = 20 + 15i$$

$$z_1^3 + z_2^3 = (z_1 + z_2)^3 - 3z_1z_2(z_1 + z_2)$$

$$z_1^3 + z_2^3 = 125 - 3z_1 \cdot z_2(5)$$

$$\Rightarrow$$
 20 + 15i = 125 - 15z₁z₂

$$\Rightarrow$$
 3z₁z₂ = 25 - 4 - 3i

$$3z_1z_2 = 21 - 3i$$

$$\mathbf{z}_1 \cdot \mathbf{z}_2 = 7 - i$$

$$(z_1 + z_2)^2 = 25$$

$$z_1^2 + z_2^2 = 25 - 2(7 - i)$$

$$(z_1^2 + z_2^2)^2 = 121 - 4 + 44i$$

$$\Rightarrow$$
 $z_1^4 + z_2^4 + 2(7-i)^2 = 117 + 44i$

$$\Rightarrow z_1^4 + z_2^4 = 117 + 44i - 2(49 - 1 - 14i)$$
$$= 21 + 72i$$

 $\Rightarrow |z_1^4 + z_2^4| = 75$

The number of solutions of $e^{\sin x} - 2e^{-\sin x} = 2$ is

(1) More than 2

(2) 2

(3) 1

(4) 0

Answer (4)

Sol. Take $e^{smx} = t (t > 0)$

$$\Rightarrow t - \frac{2}{t} = 2$$

$$\Rightarrow \frac{t^2-2}{t}=2$$

$$\Rightarrow t^2 - 2t - 2 = 0$$

$$\Rightarrow t^2 - 2t + 1 = 3$$

$$\Rightarrow (t-1)^2 = 3$$

$$\Rightarrow t = 1 \pm \sqrt{3}$$

$$\Rightarrow t = 1 \pm 1.73$$

$$\Rightarrow$$
 t = 2.73 or -0.73 (rejected as t > 0)

$$\Rightarrow e^{\sin x} = 2.73$$

$$\Rightarrow \log_{e} e^{\sin x} = \log_{e} 2.73$$

$$\Rightarrow$$
 sin x = log_e 2.73 > 1

So no solution.

 The line passes through the centre of circle $x^2 + y^2 - 16x - 4y = 0$, it interacts with the positive coordinate axis at A & B. Then find the minimum value of OA + OB, where O is origin.

(1) 20

(2) 18

(3) 12

(4) 24

Answer (1)

Sol. (y-2) = m(x-8)

⇒ x-intercept

$$\Rightarrow \left(\frac{-2}{m}+8\right)$$

⇒ y-intercept

$$\Rightarrow$$
 (-8m + 2)

$$\Rightarrow$$
 OA + OB = $\frac{-2}{m^2}$ + 8 - 8m + 2

$$f'(m) = \frac{2}{m^2} - 8 = 0$$

$$\Rightarrow m^2 = \frac{1}{4}$$

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$$\Rightarrow m = \frac{-1}{2}$$

$$\Rightarrow f\left(\frac{-1}{2}\right) = 18$$

⇒ Minimum = 18

- 11. If for some m, n; ${}^{6}C_{m} + 2\left({}^{6}C_{m+1}\right) + {}^{6}C_{m+2} > {}^{8}C_{3}$ and ${}^{n-1}P_{3}$; ${}^{n}P_{4} = 1:8$, then ${}^{n}P_{m+1} + {}^{n+1}C_{m}$ is equal to
 - (1) 6756
- (2) 7250
- (3) 6223
- (4) 6550

Answer (1)

Sol.
$${}^6C_m + 2({}^6C_{m+1}) + {}^6C_{m+2} > {}^8C_3$$

$$^{7}C_{m+1} + ^{7}C_{m+2} > ^{8}C_{3}$$

$${}^{8}C_{m+2} > {}^{8}C_{3}$$

and
$$^{n-1}P_3$$
: $^{n}P_4 = 1:8$

$$\frac{(n-1)(n-2)(n-3)}{n(n-1)(n-2)(n-3)} = \frac{1}{8}$$

$$\therefore {}^{n}P_{m+1} + {}^{n+1}C_m = {}^{8}P_5 + {}^{9}C_2$$

$$=8\times7\times6\times5\times4+\frac{9\times8}{2}$$

= 6756

- 12. Let $f: (-\infty, -1] \rightarrow (a, b]$ be defined as $f(x) = e^{x^3 + 3x + 1}$, if f is both one and onto, then the distance from a point P(2a + 4, b + 2) to curve $x + ye^{-3} 4 = 0$ is
 - (1) $\sqrt{e^3 + 2}$
- (2) $\frac{e^3 + 2}{\sqrt{e^3 + 1}}$
- (3) $\frac{e^3 + 2}{\sqrt{e^6 + 1}}$
- (4) e

Answer (3)

Sol.
$$f(x) = e^{x^3 - 3x + 1}$$

$$f'(x) = e^{x^3 - 3x + 1} \cdot (3x^2 - 3)$$

$$= e^{x^2-3x+1} \cdot 3(x-1)(x+1)$$

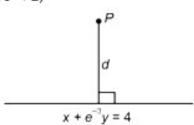
For
$$x \in (-\infty, -1]$$
, $f'(x) \ge 0$

.: f(x) is increasing function

$$\therefore \mathbf{a} = \mathbf{e}^{-x} = 0 = f(-\infty)$$

$$b = e^{-1+3+1} = e^3 = f(-1)$$

 $P(4, e^3 + 2)$

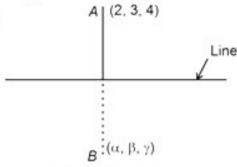


$$d = \frac{(e^3 + 2)(e^{-3})}{\sqrt{1 + e^{-6}}} = \frac{1 + 2e^{-3}}{\sqrt{1 + e^{-6}}} = \frac{e^3 + 2}{\sqrt{e^6 + 1}}$$

- 13. If (α, β, γ) is mirror image of the point (2, 3, 4) with respect to the line $\frac{x-1}{2} = \frac{y-2}{3} = \frac{z-3}{4}$. Then $2\alpha + 1$
 - $3\beta + 4y$ is
 - (1) 29
- (2) 30
- (3) 31
- (4) 32

Answer (1)

Sol.



Take
$$\frac{x-1}{2} = \frac{y-2}{3} = \frac{z-3}{4} = \lambda$$

$$x = 2\lambda + 1$$
, $y = 3\lambda + 2$, $z = 4\lambda + 3$

$$\overrightarrow{AB} = (\alpha - 2)\hat{i} + (\beta - 3)\hat{j} + (\gamma - 4)\hat{k}$$

Now.

$$(\alpha - 2) \cdot 2 + (\beta - 3) \cdot 3 + (\gamma - 4) \cdot 4 = 0$$

$$2\alpha - 4 + 3\beta - 9 + 4\gamma - 16 = 0$$

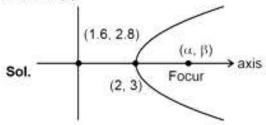
$$\Rightarrow$$
 $2\alpha + 3\beta + 4\gamma = 29$

- 14. A parabola has vertex (2, 3), equation of directrix is 2x y = 1 and equation of ellipse is $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$, $e = \frac{1}{\sqrt{2}}$ and ellipse passing through focur of parabola then square of length of latus rectum of ellipse is
 - (1) $\frac{6564}{25}$
- (2) $\frac{3288}{25}$
- (3) $\frac{6272}{25}$
- $(4) \frac{4352}{25}$



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Slope of axis =
$$\frac{1}{2}$$

$$y-3=\frac{1}{2}(x-2)$$

$$\Rightarrow$$
 2y - 6 = x - 2

$$\Rightarrow 2y - x - 4 = 0$$

$$2x + y - 6 = 0$$

$$4x + 2y - 12 = 0$$

$$\alpha + 1.6 = 4 \Rightarrow \alpha = 2.4$$

$$\beta + 2.8 = 6 \Rightarrow \beta = 3.2$$

Ellipse passes through (2.4, 3.2)

$$\Rightarrow \frac{\left(\frac{24}{10}\right)^2}{a^2} + \frac{\left(\frac{32}{10}\right)^2}{b^2} = 1$$

Also
$$1 - \frac{a^2}{b^2} = \frac{1}{2}$$

$$\frac{a^2}{b^2} = \frac{1}{2}$$

$$\frac{144}{25}b^2 + \frac{256}{25}a^2 = a^2b^2$$

$$\frac{144}{25} + \frac{256}{25} \times \frac{1}{2} = a^2$$

$$\Rightarrow \frac{(128+144)}{25} = a^2 \Rightarrow \frac{272}{25} = a^2$$

$$\Rightarrow b^2 = \frac{2 \times 272}{25}$$

Latus rectum =
$$\frac{2b^2}{a}$$

(Latus rectum)2

$$=\frac{4b^4}{a^2}=4\left(\frac{b^2}{a^2}\right)b^2=\frac{8\times272\times2}{25}=\frac{4352}{25}$$

15.

16.

17.

18.

19.

20.

SECTION - B

Numerical Value Type Questions: This section contains 10 Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

21. The value of
$$\frac{120}{\pi^3} \left| \int_{0}^{\pi} \frac{x^2 \sin x \cdot \cos x}{(\sin x)^4 + (\cos x)^4} dx \right|$$
 is

Answer (15)

Sol.
$$\int_{0}^{\pi} \frac{x^2 \sin x \cdot \cos x}{\sin^4 x + \cos^4 x} dx$$

$$= \int_{0}^{\frac{\pi}{2}} \frac{\sin x \cos x}{\sin^{4} x + \cos^{4} x} (x^{2} - (\pi - x)^{2}) dx$$

$$= \int_{0}^{\frac{\pi}{2}} \frac{\sin x \cdot \cos x (2\pi x - \pi^{2})}{\sin^{4} x + \cos^{4} x} x$$

$$=2\pi\int_{0}^{\frac{\pi}{2}}\frac{x\sin x\cos x}{\sin^{4}x+\cos^{4}x}dx-\pi^{2}\int_{0}^{\frac{\pi}{2}}\frac{\sin x\cos x}{\sin^{4}x+\cos^{4}x}dx$$

$$= 2\pi \cdot \frac{\pi}{4} \int_{0}^{\frac{\pi}{2}} \frac{\sin x \cos x}{\sin^4 x + \cos^4 x} dx - \pi^2 \int_{0}^{\frac{\pi}{2}} \frac{\sin x \cos x}{\sin^4 x + \cos^4 x} dx$$

$$=-\frac{\pi^2}{2}\int_{-\infty}^{\infty}\frac{\sin x\cos x}{\sin^4 x+\cos^4 x}dx$$

$$= -\frac{\pi^2}{2} \int_{0}^{\frac{\pi}{2}} \frac{\sin x \cos x dx}{1 - 2\sin^2 x + \cos^2 x}$$

$$= -\frac{\pi^2}{2} \int_{0}^{\frac{\pi}{2}} \frac{\frac{1}{2} \sin 2x}{1 - \frac{1}{2} \sin^2 2x} dx$$

$$= -\frac{\pi^2}{2} \int_{0}^{\frac{\pi}{2}} \frac{\sin 2x}{2 - \sin^2 2x} dx$$

$$= -\frac{\pi^2}{2} \int_{0}^{\frac{\pi}{2}} \frac{\sin 2x}{1 + \cos^2 2x} dx$$



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Let cos2x = t

$$= -\frac{\pi^2}{2} \int_{1}^{-1} \frac{1}{2} dt$$

$$= -\frac{\pi^2}{4} \int_{1}^{1} \frac{dt}{1+t^2}$$

$$=-\frac{\pi^2}{4}\cdot\frac{\pi}{2}=-\frac{\pi^3}{8}$$

$$\therefore \quad \frac{120}{\pi^3} \left| -\frac{\pi^3}{8} \right| = 15$$

 The number of ways to distribute the 21 identical apples to three children's so that each child gets at least 2 apples.

Answer (136)

Sol. After giving 2 apples to each child 15 apples left now 15 apples can be distributed in 15+3-1C₂ = 17C₂ ways

$$=\frac{17\times16}{2}=136$$

23. If A = {1, 2, 3, ... 100}, R = {(x, y) | 2x = 3y, x, y ∈ A} is symmetric relation on A and the number of elements in R is n, the smallest integer value of n is

Answer (0)

Sol. : R is symmetric relation

$$\Rightarrow$$
 $(y, x) \in R \lor (x, y) \in R$

$$(x, y) \in R \Rightarrow 2x = 3y$$
 and $(y, x) \in R \Rightarrow 3x = 2y$

Which holds only for (0, 0)

Which does not belongs to R.

24. Matrix A of order 3×3 is such that |A| = 2 $n = \underbrace{\left| adj \left(adj \left(adj \dots \left(a \right) \right) \right) \right|}_{2024 \text{ times}}$ then remainder when r

Answer (7)

divided by 9 is

Sol. |A| = 2

$$\underbrace{adj(adj(adj...(a)))}_{2024 \text{ times}} = |A|^{(n-1)^{2024}}$$

$$=\left|\mathbf{A}\right|^{2^{2024}}$$

$$2^{2024} = (2^2)2^{2022} = 4(8)^{674} = 4(9-1)^{674}$$

$$\Rightarrow$$
 $2^{2024} \equiv 4 \pmod{9}$

$$\Rightarrow$$
 2²⁰²⁴ \equiv 9m + 4, $m \leftarrow$ even

$$2^{9m+4} = 16 \cdot \left(2^3\right)^{3m} = 16 \pmod{9}$$
$$= 7$$

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