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JEE (Main)-2024 : Phase-1 (29-01-2024)-Evening

PHYSICS

SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which ONLY ONE is correct.

Choose the correct answer:

- In a simple pendulum of length 10 m, string is initially kept horizontal and the bob is released. 10% of energy is lost till the bob reaches lowermost position. Then find speed of bob at lowermost position.
 - (1) 6 m/s
 - (2) 6√5 m/s
 - (3) $7\sqrt{5}$ m/s
 - (4) 4√2 m/s

Answer (2)

Sol. $W_{\text{total}} = \Delta K$

$$\Rightarrow 0.9 mgl = \frac{1}{2} m v^2$$

$$\Rightarrow v = \sqrt{1.8 \times 10 \times 10}$$

$$= 6\sqrt{5} \text{ m/s}$$

The intensity at each slit are equal for a YDSE and it is maximum (Imax) at central maxima. If I is intensity for phase difference $\frac{7\pi}{2}$ between two waves (at screen)

Then
$$\frac{I}{I_{\text{max}}}$$
 is

- $(1) \frac{1}{2}$
- (3) $\frac{3}{9}$
- (4) $\frac{1}{\sqrt{2}}$

Answer (1)

Sol.
$$I = I_{\text{max}} \cos^2\left(\frac{\Delta\phi}{2}\right)$$

$$\frac{I}{I_{\text{max}}} = \cos^2 \frac{7\pi}{4} \qquad \qquad \because \quad \Delta \phi = \frac{7\pi}{2}$$

$$\Delta \phi = \frac{7\pi}{2}$$

$$\frac{I}{I_{\text{max}}} = \cos^2\left(\frac{\pi}{4}\right) = \frac{1}{2}$$

An electromagnetic wave has electric field given by

$$\vec{E} = (9.6\hat{j})\sin\left[2\pi\left\{30 \times 10^{6}t - \frac{1}{10}x\right\}\right]$$
, x and t are in

SI units. The maximum magnetic field is

- $(1) 3.2 \times 10^{-8}$
- $(2) 9.6 \times 10^{-8}$
- $(3) 1.7 \times 10^{-8}$
- (4) 10-7

Answer (1)

Sol.
$$\frac{E}{B} = C$$

$$\Rightarrow B = \frac{E}{C} = 3.2 \times 10^{-8}$$

A planet at distance r from sun takes 200 days to complete one revolution around sun. What will be time

period for a planet at distance $\frac{r}{4}$ from the sun?

(1) 50 days



- (2) 25 days
- (3) 100 days
- (4) 12.5 days

Answer (2)

$$\frac{200^2}{T^2} = \frac{r^3}{\left(\frac{r}{4}\right)^3}$$

$$\frac{200}{T} = (4)^{\frac{3}{2}}$$

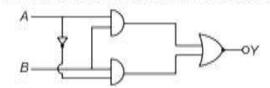
$$\frac{200}{8} = 7$$

T = 25 days

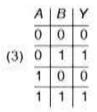
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5. The truth table for the combination of logical gates



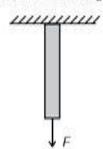
	Α	B	Y
(1)	0	0	0
	0	1	0
	1	0	0
	1	1	1



Answer (3)

Sol.
$$Y = A \cdot B + \overline{A} \cdot B = B(A + \overline{A}) = B$$

 A uniform wire has length L and radius r. It is acted on by a force F as shown. The elongation is Δl. If F and r are both halved, the new elongation will be:



- (1) $\frac{\Delta l}{2}$
- (2) A/
- (3) $4\Delta l$
- (4) 2M

Answer (4)

Sol.
$$\Delta l = \frac{FL}{Ay} \propto \frac{F}{r^2}$$

$$\Rightarrow \Delta l' = \frac{\frac{1}{2}}{\left(\frac{1}{2}\right)^2} \Delta l = 2\Delta l$$

 Two forces F₁ and F₂ are applied on two rods P and Q of same materials such that elongation in rods are same. If ratio of their radii is x : y and ratio of length is m : n, then ratio of F₁ : F₂ is

(1)
$$\left(\frac{y}{x}\right)^2 \frac{n}{m}$$

(2)
$$\left(\frac{x}{y}\right)^2 \cdot \frac{n}{m}$$

(3)
$$\left(\frac{x}{y}\right)^2 \cdot \frac{m}{n}$$

(4)
$$\left(\frac{y}{x}\right)^2 \left(\frac{m}{n}\right)$$

Answer (2)

Sol.
$$\Delta I_1 = \frac{F_1 I_1}{Y A_1}, \Delta I_2 = \frac{F_2 I_2}{Y A_2}$$

$$\frac{F_1}{F_2} = \frac{A_1}{A_2} \times \frac{I_2}{I_1} = \left(\frac{r_1}{r_2}\right)^2 \left(\frac{I_2}{I_1}\right) = \frac{x^2}{y^2} \frac{n}{m}$$

8. Two charged particles A and B have charge q each while masses are m₁ & m₂. Both have same velocity v and enter into a transverse magnetic field B such that their radii are r₁ & r₂. Then the ratio m₁: m₂ is

(1)
$$\frac{r_2}{r_1}$$

(2)
$$\left(\frac{r_1}{r_2}\right)^2$$

(3)
$$\frac{r_1}{r_2}$$

$$(4) \left(\frac{r_2}{r_1}\right)^2$$

Answer (3)

Sol.
$$t = \frac{mv}{Ba}$$

$$r \propto m \Rightarrow \frac{r_1}{r_2} = \frac{m_1}{m_2}$$

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- A liquid drop of radius R is divided into 27 identical drops. If surface tension of the drops is T, then find work done in this process.
 - (1) $4\pi R^2 T$
 - (2) $3\pi R^2 T$
 - (3) $8\pi R^2 T$
 - (4) $\frac{1}{8}\pi R^2 T$

Answer (3)

Sol. $W = T \times \text{change in area } (\Delta S)$

From volume conservation

$$\frac{4}{3}\pi R^3 = 27\pi r^3 \times \frac{4}{3}$$

R = 3r

$$r = \frac{R}{3}$$

 $\Delta S = 4\pi r^2 \times 27 - 4\pi R^2$

$$=4\pi \times \frac{R^2}{9} \times 27 - 4\pi R^2 = 2(4\pi R^2)$$

$$W = 8\pi R^2 T$$

10. Alternating voltage and current in circuit is given as

 $V = (100 \sin \omega t) \text{ volt}$

$$I = 100 \sin \left(\omega t + \frac{\pi}{3}\right) \text{mA}$$

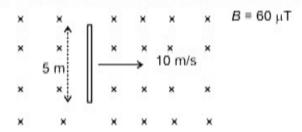
Find average power dissipated in circuit.

- (1) 2.5 W
- (2) 5 w
- (3) 10 w
- (4) 20 w

Answer (1)

Sol.
$$P_{\text{avg}} = IV \cos \phi = \frac{100}{\sqrt{2}} \times \frac{100 \times 10^{-3}}{\sqrt{2}} \cos 60^{\circ} = 2.5 \text{ w}$$

11. Consider a rod moving in a magnetic field as shown



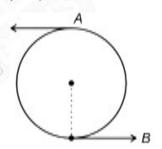
The induced emf across the ends of the rod is

- (1) 3 mV
- (2) 6 mV
- (3) 0 V
- (4) 1 mV

Answer (1)

Sol. $\varepsilon = B/v = 3 \text{ mV}$

12. A particle connected with light thread is performing vertical circular motion. Speed at point B (Lowermost point) is of just sufficient, so that it is able to complete its circular motion. Ignoring air friction, find the ratio of kinetic energy at A to that at B. (A being top-most point)



- (1) 1:5
- (2) 5:1
- (3) 1:7√2
- (4) 1:5√2

Answer (1)

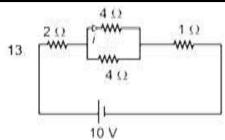
Sol.
$$V_A = \sqrt{gL}$$

$$V_B = \sqrt{5gL}$$

$$\Rightarrow \frac{k_A}{k_B} = \frac{1}{5}$$



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In given circuit, an ideal battery is connected with four resistances as shown. Find current *i* as mentioned in diagram.

- (1) 2A
- (2) 1 A
- (3) 4 A
- (4) 0.5 A

Answer (2)

Sol. req =
$$2 + 2 + 1 = 5 \Omega$$

$$t_b = \frac{10}{5} = 2 \text{ A}$$

$$1 = \frac{l_b}{2} = 1A$$

- 14
- 15.
- 16
- 17
- 18.
- 19
- 20

SECTION - B

Numerical Value Type Questions: This section contains 10 Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

 A physical quantity Q depends on other physical quantities a, b and c as

$$Q = \frac{a^4b^3}{c^2}$$

If maximum percentage error in measurement of a, b and c are 3%, 4% and 5% respectively, then find maximum percentage error in measurement of Q.

Answer (34)

Sol.
$$Q = \frac{a^4b^3}{c^2}$$

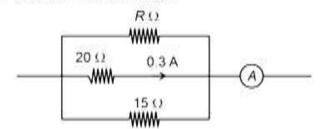
$$\frac{\Delta O}{O} = 4 \frac{\Delta a}{a} + 3 \frac{\Delta b}{b} + 2 \frac{\Delta c}{c}$$

$$\frac{\Delta Q}{Q} \times 100 = 4(3) + 3(4) + 2(5)$$

= 12 + 12 + 10

% error
$$\frac{\Delta Q}{Q}$$
% = 34%

22 Consider the circuit shown



The ammeter reads 0.9 A. Value of R is _____

Answer (30)

Sol. 20 \Omega & 15 \Omega in parallel

$$\Rightarrow$$
 20 × 0.3 = 15 × /

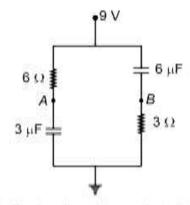
$$\Rightarrow i_R = 0.9 - 0.3 - 0.4 \text{ A}$$

$$= 0.2 A$$

$$\Rightarrow R \times 0.2 = 20 \times 0.3$$

$$A \Rightarrow R = 30 \Omega$$

23. Consider the circuit shown:



Charge on 6 μF when A and B are shorted is _____ μC

Answer (36)

Sol. In steady state, 6Ω and 3Ω are in series.

$$\Rightarrow \Delta V_{6\Omega} = 6 V = \Delta V_{6\mu}F$$

$$\Rightarrow \phi = CV = 36 \mu C$$

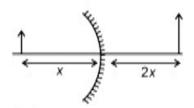
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 Distance between twice-magnified virtual image of an object placed in front of mirror is 15 cm. Find focal length of spherical mirror in cm.

Answer (10)

- Sol. Magnified virtual image of real object
 - ⇒ Concave mirror



$$\left(\frac{\mathbf{v}}{u}\right) = 2$$

$$\Rightarrow$$
 2x + x = 15

$$x = 5 \text{ cm}$$

$$\frac{1}{v} + \frac{1}{u} = \frac{1}{t}$$

$$\Rightarrow \frac{1}{10} - \frac{1}{5} = \frac{1}{f}$$

$$\frac{1-2}{10} = \frac{-1}{10} = \frac{1}{t}$$

$$\Rightarrow f = -10$$

25. The displacement of a particle changing with time as x = 6t³ - 12t² + 20t + 30. Find velocity (in m/s) of particle when it's acceleration became zero. (t is time in s)

Answer (12)

Sol.
$$v = \frac{dx}{dt} = 20$$

$$= 18t^2 - 24t + 20$$

$$a = \frac{dv}{dt} = 36t - 24$$

At
$$a = 0$$

$$t = \frac{24}{36} = \frac{2}{3}$$
 sec

Then.

$$v = 18 \times \frac{4}{9} - 24 \times \frac{2}{3} + 20$$

$$= 8 - 16 + 20 = 12 \text{ m/s}$$

26. Electric field in a region is given by $\dot{E} = (6\hat{i} + 7\hat{j} + 8\hat{k})$ units. An area of 30 units is considered in *y-z* plane. Calculate the electric flux through this area.

Answer (180)

Sol.
$$\phi = \vec{E} \cdot \vec{A} = (6\hat{i} + 7\hat{j} + 8\hat{k}) \cdot 30\hat{i} = 180$$

27. N moles of non-linear polyatomic gas (degree of freedom 6) is mixed with 2 moles of monoatomic gas. The resultant mixture has molar specific heal equal to that of a diatomic gas, then N is

Answer (4)

Sol.
$$\frac{n_1 \frac{f_1}{2} R + n_2 \frac{f_2}{2} R}{n_1 + n_2} = \frac{5}{2} R$$

$$\frac{2 \times \frac{3}{2}R + N \times \frac{6}{2}R}{N+2} = \frac{5}{2}R$$

$$\frac{6+6N}{N+2}=5$$

$$6 + 6N = 5N + 10$$

$$N = 4$$

28. A particle starts oscillation from origin on x-axis with period of oscillation (6) sec and amplitude A. If time

taken by particle to reach from x = A to $x = \frac{\sqrt{3}}{2}A$

for the first time is τ then. Value of 6τ is _____ sec

Answer (3)

Sol.
$$x = A \sin\left(\omega t + \frac{\pi}{2}\right)$$

$$x = A\cos\omega t$$

$$\frac{\sqrt{3}}{2}A = A\cos\left(\frac{2\pi}{\tau}t\right)$$

$$\frac{\sqrt{3}}{2} = \cos\left(\frac{\pi}{3}t\right)$$

$$\frac{\pi}{6} = \frac{t}{3}\pi$$

$$t = \frac{1}{2} = 0.5$$

$$6\tau = 3$$

29.

30

CHEMISTRY

SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which ONLY ONE is correct.

Choose the correct answer:

- Best reducing agent among the given ions is
 - (1) Ce4+
- (2) Gd2+
- (3) Lu3+
- (4) Nd3+

Answer (2)

Sol. Gd2+ : [Xe] 5d14f7

Gd2+ would get converted into Gd3+ as Gd3+ has stable electronic configuration

Choose the correct reaction. 2

(2)
$$\bigcirc \xrightarrow{Br} \bigcirc Br$$

Answer (4)

$$CH_{3}-CH_{2}-CH_{2}-CH_{3}-CH_{3}-CH_{3}-CH_{3}$$

$$CH_{3}-CH_{2}-CH_{2}-CH_{2}-CH_{3}-CH_{3}$$

$$CH_{3}-CH_{2}-CH_{2}-CH_{3}-CH_{3}$$

$$CH_{3}-CH_{2}-CH_{3}-CH_{3}$$

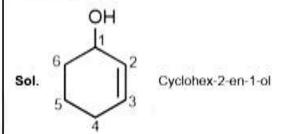
$$CH_{3}-CH_{3}-CH_{3}-CH_{3}$$

IUPAC name of compound



- (1) Hex-2-en-1-ol
- (2) Cyclohex-2-en-1-ol
- (3) 3-hydroxy cyclohexene
- (4) Cyclohex-1-en-3-ol

Answer (2)



- Why does oxygen shows anomalous behaviour?
 - (1) Large size, high electronegativity
 - (2) Small size, small electronegativity
 - (3) Small size, high electronegativity absence of vacant d-orbital
 - (4) Large size, high electronegativity presence of vacant d-orbital

Answer (3)

- Sol. Oxygen shows anomalous behaviour due to small size, high electronegativity and absence of vacant d-orbital.
- Match the following
 - (A) Lyman
- (i) IR
- (B) Balmer
- (ii) IR
- (C) Paschen
- (iii) Visible
- (D) Pfund
- (iv) UV
- (1) $A \rightarrow (iv)$, $B \rightarrow (iii)$
 - $C \rightarrow (i), D \rightarrow (ii)$
- (2) $A \rightarrow (i)$, $B \rightarrow (iii)$
 - $C \rightarrow (ii)$, $D \rightarrow (iv)$



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(3) $A \rightarrow (iv)$, $B \rightarrow (ii)$

 $C \rightarrow (iii), D \rightarrow (iv)$

(4) $A \rightarrow (i)$, $B \rightarrow (ii)$

 $C \rightarrow (iii), D \rightarrow (iv)$

Answer (1)

Sol. Lyman → UV

Balmer → Visible

Paschen → IR

Pfund → IR

- IUPAC name of K₂MnO₄ is
 - Potassium tetraoxomanganate(VI)
 - (2) Potassium tetraoxomanganate(III)
 - (3) Potassium tetraoxomanganese(VI)
 - (4) Tetraoxomanganese(VI) potassium

Answer (1)

Sol. Correct IUPAC name of K₂MnO₄ is Potassium tetraoxomanganate(vi)

Find out final product (A)

(1)
$$\bigcirc$$
 (2) \bigcirc NH₂ CI (1) \bigcirc (2) \bigcirc NH₂ CI (3) \bigcirc (4) \bigcirc CI

Answer (3)

Sol.
$$\bigcap_{\text{Diazotisation}}^{\text{NH}_2} \bigcap_{\text{Cu}_2\text{Cl}_2/\text{HCl}}^{\text{N}} \bigcap_{\text{Cl}}^{\text{Cl}} \bigcap_{\text{Cl}}^{\text{$$

- Which of the following element has highest 1st lonization energy?
 - (1) N

- (2) C
- (3) Si
- (4) Al

Answer (1)

Sol. N has highest 1st Ionization energy among C, Si, N and Al.

For, $N = 1402 \text{ kJ mol}^{-1} (IE_1)$

 $C = 1086 \text{ kJ mol}^{-1} (IE_1)$

 $AI = 577 \text{ kJ mol}^{-1} (IE_1)$

 $Si = 786 \text{ kJ mol}^{-1} (IE_1)$

- Which reagent gives bright red ppt with Ni²⁺ in basic medium?
 - (1) DMG
- (2) Nessler's reagent
- (3) KCNS
- (4) K₄[Fe(CN)₆]

Answer (1)

Sol. NiCl, + CH, - C = NOH
$$CH, - C = NOH$$

$$CH, - C = NOH$$

$$DMG$$

$$Dimethylglyoxime
$$(Cherry red ppt.)$$

$$(Bright red)$$$$

10. Match the following List-I and List-II

	List-I (Polymer)		List-II (Monomer)
(A)	Starch	(i)	β-glucose
(B)	Cellulose	(ii)	Nucleotide
(C)	Nucleic acid	(iii)	α-glucose
(D)	Protein	(iv)	α-Amino acid

- (1) $A \rightarrow (i)$; $B \rightarrow (iii)$, $C \rightarrow (ii)$; $D \rightarrow (iv)$
- (2) $A \rightarrow (iii)$; $B \rightarrow (i)$, $C \rightarrow (ii)$; $D \rightarrow (iv)$
- (3) $A \rightarrow (iii)$, $B \rightarrow (i)$, $C \rightarrow (iv)$, $D \rightarrow (ii)$
- (4) $A \rightarrow (ii)$; $B \rightarrow (iii)$; $C \rightarrow (i)$; $D \rightarrow (iv)$

Answer (2)

Sol. Starch is polymer of α-D-glucose. Cellulose is polymer of β-D-glucose. Nucleic acid is polymer of nucleotide. Proteins are polymer of α-aminoacids.

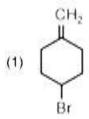
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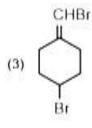
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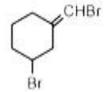
11. Which of the following can show geometrical isomerism?

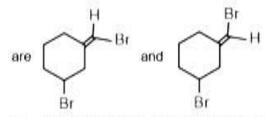




Answer (4)

Sol. The two geometrical isomers of





- 12 Which reagent is used to convert alkyl halide into alkyl isocyanide?
 - (1) KCN
- (2) AgCN
- (3) KNO₂
- (4) AgNO₂

Answer (2)

Sol. $R - X + AqCN \rightarrow R - N = C + AqX$

- Find the total number of sigma (σ) and π bonds in 2-formylhex-4-enoic acid
 - (1) 20
- (2) 22
- (3) 18
- (4) 24

Answer (2)

Sol. The structure of 2-formylhex-4-enoic acid is

H—O—C—C—CH,—CH = CH—CH,
$$n - bonds = 19$$

C—H

- 14 A gas 'X' is added to Nessler's reagent then brown precipitate is formed, gas X is
 - (1) NH₃
- (2) SO₂
- (3) Cl₂
- (4) Br2

Answer (1)

Sol. 2K₂Hgl₄+3KOH+NH₃ → Nessler's

Nessler's reagent

 $\begin{bmatrix} \mathsf{OHg}_2 \ \mathsf{NH}_2 \end{bmatrix} \mathsf{I} + \mathsf{7KI} + \mathsf{2H}_2 \mathsf{O} \\ \mathsf{Brown ppt} \end{bmatrix}$

Ammonia gas on reaction with Nessler's reagent to form brown ppt. Brown ppt formed is also called iodide of million's base (H₂N — Hg — O — Hg — I)

15. Match the following

I (compounds)		II (pKa)		
(a)	p-nitrophenol	(i)	10	
(b)	m-nitrophenol	(11)	16	
(c)	Ethanol	(111)	7.1	
(d)	Phenol	(iv)	8.3	

- (1) (a) \rightarrow (i), (b) \rightarrow (ii), (c) \rightarrow (iii), (d) \rightarrow (iv)
- (2) (a) \rightarrow (iii); (b) \rightarrow (iv), (c) \rightarrow (ii), (d) \rightarrow (i)
- (3) (a) \rightarrow (iv), (b) \rightarrow (iii), (c) \rightarrow (ii), (d) \rightarrow (i)
- (4) (a)→(iii); (b)→(iV); (c)→(i); (d)→(ii)

Answer (2)

Sol. Acidic strength order

p-nitrophenol > m-nitrophenol > Phenol >> ethanol

16. We have given some hydrocarbons

- (A) HC = CH
- (B) $H_2C = CH_2$

(D) CH₃ − CH₂ − CH₂ − H

Correct order of acidic strength of above hydrocarbons

- (1) A>B>C>D
- (2) A>B>D>C
- (3) C > D > B > A
- (4) A>C>B>D

Answer (2)

Sol. More the stability of conjugate base of given acids, more will be the acidic strength.

(A) HC ≡ C (more % s character more will be stability of anion)

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density on carbon so stability decreases)

So order of acidic strength

- 17 In chromatographic techniques, which of the following follows preferential adsorption?
 - (A) Column chromatography
 - (B) Thin layer chromatography
 - (C) Paper chromatography
 - (1) A only
- (2) Bonly
- (3) Conly
- (4) A and B both

Answer (4)

Sol. Column chromatography Separation based on Thin layer chromatography absorption of substance

Paper chromatography → Partition chromatography

18. Consider the following sequence of reactions

Fina A, B and C

- (1) A DIBAL-H
 - B: NaOH (dil)
 - C: Zn Hg/HCI
- (2) A LIAIH4
 - B: KOH (alcoholic)
 - C: NH2 NH2/KOH
- (3) A: DiBAL H
 - B: NaOH (dil)
 - C: NH2 NH2/KOH
- (4) A NaBH₄
 - B. KOH (aqueous)
 - C: Zn Hg/HCI

Answer (3)

- Sol. (A) DiBALH Convert ester to aldehyde
 - (B) dil NaOH Aldol condensation
 - (C) NH2 NH2/KOH Wolff Kishner reduction
- 19. The correct statement about Zn, Cd, Hg are
 - (1) All are solid metals at room temperature
 - (2) They have high enthalpy of atomization
 - (3) All are paramagnetic
 - (4) Zn, Cd cannot show variable oxidation state but Hg can show variable oxidation state

Answer (4)

Sol. Hg can show +1 and +2 O.S.

The major product in the above reaction is

- 2-hydroxybenzaldehyde
- (2) 2-hydroxybenzoic acid
- (3) 4-hydroxybenzaldehyde
- (4) 3-hydroxybenzaldehyde

Answer (1)

is the major product in Reimer-

Tiemann reaction

SECTION - B

Numerical Value Type Questions: This section contains 10 Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

 Oxidation state of Fe (Iron) in complex formed in brown ring test.

Answer (1)

Sol. Complex formed during brown ring test is [Fe(H₂O)₅NO]SO₄.

NO is present as NO' here.

$$x + 5 \times 0 + 1 = +2$$

x = +1

Oxidation state of Fe is +1

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22. How many of the following compounds have zero dipole moment?

NH3, H2O, HF, CO2, SO2, BF3, CH4

Answer (3)

Sol. CO₂, BF₃ and CH₄ have symmetrical structures leading to μ = O

Calculate equilibrium constant for the given following reaction at 500K.

$$N_2(g) + 3H_2(g)$$
. $-2NH_3(g)$

Given molarity of NH₂(g), N₂(g) and H₂(g) at equilibrium is 1.5×10^{-2} M, 2×10^{-2} M and 3×10^{-2} M respectively.

Answer (417)

Sol.
$$K_C = \frac{[NH_3]^2}{[N_2][H_2]^3}$$

$$K_C = \frac{(1.5 \times 10^{-2})^2}{(2 \times 10^{-2}) \times (3 \times 10^{-2})^3}$$

$$K_C = \frac{2.25 \times 10^{-4}}{2 \times 10^{-2} \times 27 \times 10^{-6}}$$

$$K_C = 0.04167 \times 10^4$$

$$K_C = 416.7 \approx 417$$

 50 ml of 0.5 M oxalic acid is completely Neutralised by 25 ml of NaOH solution. Find out amount of NaOH (in gm) present in 25 ml of given NaOH solution.

Answer (2)

Sol.
$$M_1V_1N_1 = M_2V_2N_2$$

$$(50)(0.5)(2) = (M_2)(25)(1)$$

$$M_2 = 2$$

Moles of NaOH =
$$\frac{2 \times 25}{1000} = \frac{1}{20}$$

Mass of NaOH =
$$\frac{1}{20} \times 40 = 2gm$$

 If standard enthalpy of vaporization of CCI₄ is 30.5 kJ/mol, find heat absorbed for vaporization of 294 gm of CCI₄. [Nearest integer] [in kJ]

Answer (58)

Sol. Vaporization of 1 mole CCI₄ requires 30.5 kJ

294 gm is
$$\frac{294}{154}$$
 = 1.91 moles

Vaporization of 1.91 moles of CCI₄ will require 30.5 × 1.91 kJ = 58.255 kJ

 Find out molality of 0.8 M H₂SO₄ solution having density of solution equal to 1.02 gm/ml (Nearest integer)

Answer (1)

Sol.
$$m = \frac{1000 \text{ M}}{10008 - \text{M} (\mu)}$$

= $\frac{1000 (0.8)}{1000 (1.02) - (0.8) (98)} = \frac{800}{1020 - 78.4}$
= $\frac{800}{941.6} = 0.849$

 Aqueous solution of [AuCl₄]⁻ on electrolysis by passing current for 10 minutes, the mass of Au deposited at Cathode is 1.97 gm. Find out current required (in A) (Nearest integer)

Answer (5)

$$\frac{1.97}{197} = 0.01 \,\text{mole}$$

Charge =
$$0.03 \times 96500$$

$$Current = \frac{0.03 \times 96500}{10 \times 60}$$

 If half life of radioactive bromine (Br-82) is 36 hr, find percentage remaining after one day. [nearest integer]

Answer (63)

Sol.
$$ln \frac{N_0}{N} = \lambda t = \frac{ln 2}{36} \times 24$$

$$=\frac{2}{3}\ln 2$$

$$\Rightarrow \frac{N_0}{N} = 2^{2/3}$$

$$\Rightarrow \frac{N}{N_0} = \frac{1}{2^{2/3}}$$

% age remaining =
$$100 \frac{N}{N_0} = \frac{100}{2^{2/3}} = 62.99$$

29

30

MATHEMATICS

SECTION - A

Multiple Choice Questions: This section contains 20 multiple choice questions. Each question has 4 choices (1), (2), (3) and (4), out of which ONLY ONE is correct.

Choose the correct answer :

Given set = $\{1, 2, 3, ..., 50\}$

One number is selected randomly from set. Find probability that number is multiple of 4 or 6 or 7

- (3)

Answer (1)

Sol. Take P(A) = Probability that number is multiple of 4

P(B) = Probability that number is multiple of 6

P(C) = Probability that number is multiple of 7

$$P(A) = \frac{12}{50}, P(B) = \frac{8}{50}, P(C) = \frac{7}{50}$$

$$P(A \cap B) = \frac{4}{50}$$
 (Multiple of 12)

$$P(B \cap C) = \frac{1}{50}$$
 (Multiple of 42)

$$P(A \cap C) = \frac{1}{50}$$
 (Multiple of 28)

 $P(A \cap B \cap C) = 0$ (Multiple of 84)

$$P(A \cup B \cup C) = P(A) + P(B) + P(C) - P(A \cap B) - P(B \cap C) - P(A \cap C) + P(A \cap B \cap C)$$

$$= \frac{12}{50} + \frac{8}{50} + \frac{7}{50} - \frac{4}{50} - \frac{1}{50} + 0$$

$$=\frac{21}{50}$$

$$2 \int_{6}^{3} \sqrt{1 - \sin 2x} \, dx \text{ is}$$

- (1) $\sqrt{2} \sqrt{3} + 1$ (2) $2\sqrt{2} \sqrt{3} 1$
- (3) $2\sqrt{2} + \sqrt{3} 1$ (4) $\sqrt{2} + \sqrt{3} 1$

Answer (2)

Sol.
$$\int_{0}^{3} |\sin x - \cos x| dx$$

$$= \int_{a}^{\pi} (\cos x - \sin x) dx + \int_{a}^{\pi} (\sin x - \cos x) dx$$

$$= (\sin x + \cos x)_{\pi}^{\pi} + (-\sin x - \cos x)_{\pi}^{3}$$

$$= \left[\left(\frac{1}{\sqrt{2}} + \frac{1}{\sqrt{2}} \right) - \left(\sin \frac{\pi}{6} + \cos \frac{\pi}{6} \right) \right] + \left[\left(-\sin \frac{\pi}{3} - \cos \frac{\pi}{3} \right) - \left(-\sin \frac{\pi}{4} + \cos \frac{\pi}{4} \right) \right]$$

$$= \left[\sqrt{2} - \left(\frac{1}{2} + \frac{\sqrt{3}}{2} \right) \right] + \left[-\frac{\sqrt{3}}{2} - \frac{1}{2} + \frac{1}{\sqrt{2}} + \frac{1}{\sqrt{2}} \right]$$

$$=2\sqrt{2}-\sqrt{3}-1$$

- A = (1, 2, 3, 4) minimum number of elements added to make it equivalence relation on set A containing (1, 3) and (1, 2) in it.
 - (1) 8
- (2)9
- (3) 12
- (4) 16

Answer (1)

Sol. Set A = {1, 2, 3, 4}

For reflexive relation

We need to have (1, 1), (2, 2), (3, 3), (4, 4).

For symmetric,

(1, 3) ∈A

So (3, 1) should be added

And $(1, 2) \in A$

So (2, 1) should be added

set has become ((1, 1), (2, 2), (3, 3), (4, 4), (1, 3),

(3, 1), (1, 2), (2, 1))

Now $(3, 1) \in A$

(1, 2) ∈A

So (3, 2) should be added (for transitive)

Then (2, 3) should be added (for symmetric)

So set becomes

{(1, 1), (2, 2), (3, 3), (4, 4), (1, 3), (3, 1), (1, 2), (2, 1), (3, 2), (2, 3))

So minimum 8 elements are added



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- If In a, In b, In c are in AP and In a In 2b, In 2b -In 3c, In 3c -In a are in AP then a : b : c is
 - (1) 1:2:3
- (2) 7:7:4
- (3) 9:9:4
- (4) 4:4:9

Answer (3)

Sol. $\ln a$, $\ln b$, $\ln c \rightarrow AP$

$$\Rightarrow b^2 = ac$$

$$\ln \frac{a}{2b}$$
, $\ln \frac{2b}{3c}$, $\ln \frac{3c}{a}$

$$\left(\frac{2b}{3c}\right)^2 = \frac{a}{2b} \times \frac{3c}{a}$$

$$\frac{4b^2}{9c^2} = \frac{3c}{2b}$$

$$8b^3 = 27c^3$$

$$2b = 3c$$

...(ii)
$$\Rightarrow 4b = 9c$$

$$4b^2 = 9c^2$$

$$4ac = 9c^2$$

$$\Rightarrow 4a - 9c$$

From (ii) & (iii)

$$4a = 9c = 4b = k$$

$$a = \frac{k}{4}b = \frac{k}{4}c = \frac{k}{9}$$

$$a:b:c=\frac{1}{4}:\frac{1}{4}:\frac{1}{9}$$

$$a:b:c=9:9:4$$

- If r = |z|, $\theta = \arg(z)$ and $z = 2 2i \tan\left(\frac{5\pi}{8}\right)$ then find
 - (1) $\left(2\sec\frac{5\pi}{8}, \frac{3\pi}{8}\right)$ (2) $\left(2\sec\frac{3\pi}{8}, \frac{3\pi}{8}\right)$
 - (3) $\left(2\tan\frac{3\pi}{8}, \frac{5\pi}{8}\right)$ (4) $\left(2\tan\frac{3\pi}{8}, \frac{3\pi}{8}\right)$

Answer (2)

$$z = 2 - 2i \frac{\sin \frac{5\pi}{8}}{\cos \frac{5\pi}{8}}$$
$$= \frac{2}{\cos \frac{5\pi}{8}} \left(\cos \frac{5\pi}{8} - i \sin \frac{5\pi}{8}\right)$$
$$2 \qquad ext{1/3}$$

$$=2\sec\left(\frac{5\pi}{8}\right)e^{i\frac{(-5\pi)}{8}}$$

$$=2\sec\left(\frac{3\pi}{8}\right)e^{it}e^{i\frac{(-5\pi)}{8}}$$

$$=2\sec\frac{3\pi}{8}e^{i\frac{(3\pi)}{8}}$$

$$\theta = \frac{3\pi}{8}$$
, $r = 2\sec\frac{3\pi}{8}$

- In which interval the function $f(x) = \frac{x}{x^2 6x 16}$ is increasing?
 - (1) ¢

- (2) $\left[1, \frac{3}{4}\right] \cup \left(\frac{5}{4}, \infty\right)$
- (3) $\left(\frac{5}{4}, \infty\right)$
- (4) $\left[\frac{3}{4}, \frac{5}{4}\right]$

Answer (1)

Sol.
$$f(x) = \frac{x}{x^2 - 6x - 16}$$

$$f'(x) = \frac{(x^2 - 6x - 16) - (x)(2x - 6)}{(x^2 - 6x - 16)^2}$$

$$\Rightarrow \frac{-x^2-16}{(x^2-6x-16)^2} < 0 \ \forall \ x \in D,$$

- (α, β) lie on the parabola $y^2 = 4x$ and (α, β) also lie on chord with mid-point $\left(1, \frac{5}{4}\right)$ of another parabola
 - $x^2 = 8y$, then value of $\lfloor (8 \beta)(\alpha 28) \rfloor$ is
 - (1) 192
- (2)92
- (3) 64
- (4) 128

Answer (1)

Sol. Chord with point, $T = S_1$

$$\Rightarrow xx_1 - 4(y + y_1) = x_1^2 - 8y_1$$

$$(x_1, y_1) = \left(1, \frac{5}{4}\right) \implies x - 4\left(y + \frac{5}{4}\right) = \frac{1 - 8 \times 5}{4}$$

$$x - 4y - 5 = -9$$

$$\Rightarrow x - 4y + 4 = 0$$

 (α, β) lie on (L1) and also $y^2 = 4x$

$$\Rightarrow \alpha - 4\beta + 4 = 0$$

$$\beta^2 = 4\alpha$$

$$\beta^2 = 4(4\beta - 4)$$

$$\beta^2 - 16\beta + 16 = 0$$



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$$\Rightarrow (\beta - 8)^2 = 64 - 16 = 48$$

$$\Rightarrow \beta = 8 \pm 4\sqrt{3}$$

$$\alpha = 4\beta - 4$$

$$= 28 \pm 16\sqrt{3}$$

$$(28 + 16\sqrt{3}, 8 + 4\sqrt{3})$$
 and $(28 - 16\sqrt{3}, 8 - 4\sqrt{3})$

$$(8 - \beta)(\alpha - 28)$$

$$\Rightarrow (-4\sqrt{3})(16\sqrt{3})$$

$$= -192$$

8. Unit vector
$$\vec{u} = x\hat{i} + y\hat{j} + z\hat{k}$$
 makes angles

$$\frac{\pi}{2}$$
, $\frac{\pi}{3}$, $\frac{2\pi}{3}$ with $\left(\frac{1}{\sqrt{2}}\tilde{i} + \frac{1}{\sqrt{2}}\tilde{k}\right)$, $\left(\frac{1}{\sqrt{2}}\tilde{j} + \frac{1}{\sqrt{2}}\tilde{k}\right)$.

$$\left(\frac{\hat{i}}{\sqrt{2}} + \frac{\hat{j}}{\sqrt{2}}\right)$$
 respectively and

$$\vec{v} = \frac{1}{\sqrt{2}}\hat{i} + \frac{1}{\sqrt{2}}\hat{j} + \frac{1}{\sqrt{2}}\hat{k} \text{ find } |\vec{u} = \vec{v}|.$$

(1)
$$\sqrt{\frac{5}{2}}$$

(2)
$$\sqrt{\frac{7}{2}}$$

(3)
$$\sqrt{\frac{2}{5}}$$

(4)
$$\sqrt{\frac{2}{7}}$$

Answer (1)

Sol.
$$\frac{x}{\sqrt{2}} + \frac{z}{\sqrt{2}} = 0$$

$$\frac{y}{\sqrt{2}} + \frac{z}{\sqrt{2}} = \frac{1}{2}$$

(2)

$$\frac{x}{\sqrt{2}} + \frac{y}{\sqrt{2}} = \frac{-1}{2}$$

...(3)

$$\Rightarrow y=0, z=\frac{1}{\sqrt{2}}, x=\frac{-1}{\sqrt{2}}$$

$$\vec{v} - \vec{u} = \sqrt{2}\hat{i} + \frac{1}{\sqrt{2}}\hat{j}$$

$$\left|\vec{v} - \vec{u}\right| = \sqrt{2 + \frac{1}{2}}$$

$$=\sqrt{\frac{5}{2}}$$

9. If first term of non-constant GP be $\frac{1}{8}$ and every

term is AM of next two, then $\sum_{\ell=1}^{20} T_{\ell} - \sum_{\ell=1}^{18} T_{\ell}$ is

$$(2) -2!$$

$$(3) -2^{18}$$

$$(4) 2^{18}$$

Answer (2)

Sol.
$$a_1 = \frac{1}{8}$$

a, ar, ar², ar³

$$2ar = ar^2 + ar^3$$

$$2 = r + r^2$$

$$r^2 + r - 2 = 0$$

$$(r+2)(r-1)=0$$

$$\Rightarrow r = -2$$

$$\sum_{r=1}^{20} T_r - \sum_{r=1}^{18} T_r$$

$$=\frac{a(1-r^{20})}{1-r}-\frac{a(1-r^{18})}{1-r}$$

$$= \frac{1}{8} \left[\frac{1}{3} \left[1 - r^{20} - 1 + r^{18} \right] \right]$$

$$=\frac{1}{24}2^{18}[1-4]$$

$$=-\frac{2^{18}}{8} \Rightarrow -2^{15}$$

10. The mean of 5 observations is $\frac{24}{5}$ and variance is

 $\frac{194}{25}$. If the mean of first four observations is $\frac{7}{2}$

then the variance of first four observations is

(1)
$$\frac{3}{2}$$

(3)
$$\frac{5}{4}$$

(4)
$$\frac{2}{3}$$

Answer (3)

Sol.
$$\sum_{i=1}^{5} x_i = 24$$

$$\frac{\sum x_i^2}{5} - \left(\frac{24}{5}\right)^2 = \frac{194}{25}$$

$$\Rightarrow \sum x_i^2 = \frac{770}{25} \times 5 = 154$$

$$5^{th}$$
 observation = $24 - \frac{7}{2} \times 4 = 10$

New variance
$$= \frac{\sum_{i=1}^{4} x_i^2}{4} - \left(\frac{7}{2}\right)^2$$
$$= \frac{154 - 100}{4} - \frac{49}{4}$$
$$= \frac{5}{4}$$



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11.

12.

13.

14.

15.

16.

17.

18.

19.

20

SECTION - B

Numerical Value Type Questions: This section contains 10 Numerical based questions. The answer to each question should be rounded-off to the nearest integer.

21. The remainder when $64^{32^{32}}$ is divided by 9 is

Answer (1)

Sol. $64 = 1 \pmod{9}$

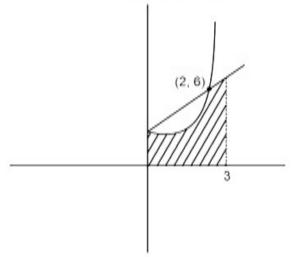
$$64^{32^{32}} = 1^{32^{32}} \pmod{9}$$

⇒ Remainder = 1

22 Area bounded by $0 \le y \le \min \{x^2 + 2, 2x + 2\}, x \in [0, 3]$ is A, then 12 A is

Answer (164)

Sol.
$$\min\{x^2+2, 2x+2\}\begin{cases} x^2+2 & 0 \le x \le 2\\ 2x+2 & 2 \le x \le 3 \end{cases}$$



Area =
$$A = \int_{0}^{2} (x^{2} + 2)dx + \frac{1}{2}[6 + 8] \times 1$$

$$=\frac{x^3}{3}+2x\Big|_0^2+7$$

$$\frac{8}{3} + 4 + 7 = \left(\frac{8}{3} + 11\right)$$
 unit

$$12A = 12\left(\frac{8}{3} + 11\right) = 164$$

 The number of ways to distribute 8 identical books into 4 distinct bookshelf is (where any bookshelf can be empty)

Answer (165)

Sol.
$$x_1 + x_2 + x_3 + x_4 = 8$$

Number of ways =
$$\binom{8+4-1}{4-1}$$

$$= \binom{11}{3}$$

24. If
$$f(x) = \ln\left(\frac{1-x^2}{1+x^2}\right)$$
 then value of $225(f'(x) - f''(x))$

at
$$x = \frac{1}{2}$$

Answer (736)

Sol.
$$f(x) = \ln(1 - x^2) - \ln(1 + x^2)$$

$$f'(x) = \frac{-2x}{1-x^2} - \frac{2x}{1+x^2}$$

$$=-2x\left[\frac{2}{1-x^4}\right]$$

$$f'(x) = \frac{4x}{x^4 - 1}$$

$$f''(x) = 4 \left[\frac{(x^4 - 1) - 4x^4}{(x^4 - 1)^2} \right]$$

$$=4\left[\frac{-3x^4-1}{(x^4-1)^2}\right]$$

$$f'(x) - f''(x) = 4 \left[\frac{x}{x^4 - 1} + \frac{3x^4 + 1}{(x^4 - 1)^2} \right]$$

At
$$x = \frac{1}{2}$$

$$225[f'(x) - f''(x)] = 736$$



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25.
$$\frac{3\cos 2x + \cos^3 2x}{\cos^6 x - \sin^6 x} = x^3 - x^2 + 6$$
, then find sum of

Answer (1)

Sol. :

$$\frac{\cos 2x(3 + \cos^2 2x)}{(\cos^2 x - \sin^2 x)[\sin^4 x + \cos^4 x + \sin^2 x \cos^2 x]},$$
$$\cos^2 x - \sin^2 x = \cos 2x$$

$$= \frac{3 + \cos^2 2x}{1 - \sin^2 x \cos^2 x} = 4 \left(\frac{3 + \cos^2 2x}{4 - \sin^2 2x} \right) = 4$$

$$\Rightarrow x^3 - x^2 + 6 = 4$$

$$\Rightarrow x^3 - x^2 + 2 = 0$$

: therefore sum of roots = 1

26.
$$x \left(\cos\left(\frac{y}{x}\right)\right) \frac{dy}{dx} = y\cos\left(\frac{y}{x}\right) + x$$

where
$$\sin\left(\frac{y}{x}\right) = \ln|x| + \frac{\alpha}{2}$$
 and $f(1) = \frac{\pi}{3}$

Find α^2 .

Answer (3)

Sol.
$$\because \left(\cos\frac{y}{x}\right)\frac{dy}{dx} = \frac{y}{x}\cos\frac{y}{x} + 1$$

Putting v = vx

$$\Rightarrow \frac{dy}{dx} = x \frac{dv}{dx} + v$$

$$\Rightarrow \cos v \left(x \frac{dv}{dx} + v \right) = v \cos v + 1$$

$$\Rightarrow \int \cos v dv = \int \frac{dx}{x}$$

$$\Rightarrow \sin \frac{y}{x} = \ln |x| + c$$

where
$$c = \frac{\alpha}{2}$$

putting initial condition,

$$2\sin\frac{\pi}{3} = \alpha$$

$$\Rightarrow \alpha = \sqrt{3}$$

$$\Rightarrow \alpha^2 = 3$$

27. If
$$\overline{OA} = \vec{a}$$
, $\overline{OC} = \vec{b}$, and area of $\triangle OAC$ is S and a parallelogram with sides parallel to \overline{OA} and \overline{OC} and diagonal $\overline{OB} = 12\vec{a} + 4\vec{b}$, has area equal to B , then $\frac{B}{S}$ is equal to

Answer (96)

Sol.
$$S = \frac{1}{2} |\vec{a} \times \vec{b}|$$

$$B = \left| 12\vec{a} \times 4\vec{b} \right|$$

$$\Rightarrow \frac{B}{S} = \frac{48|\vec{a} \times \vec{b}|}{\frac{1}{2}|\vec{a} \times \vec{b}|} = 96$$

28.

29

30.